

Jan 23, 17 10:47 **p3n162B** Page 1/2

```
-->// Mat01186 - P3 2016/2 B
-->// Questao 1 Quadratura Composta de Simpson
-->// comecaremos na ponta superior, no sentido horario
o
-->a=2.65; I1 = (0 + 4*4.78 + 6.0)*a/3
I1 =
22.189333

-->I2 = (6.0 + 4*6.14 + 4.55)*a/3
I2 =
31.013833

-->I3 = (4.55 + 4*2.95 + 0)*a/3
I3 =
14.4425

-->I4 = (0 + 4*2.27 + 4.55)*a/3
I4 =
12.039833

-->I5 = (4.55 + 4*5.0 + 3.3)*a/3
I5 =
24.600833

-->I6 = (3.3 + 4*3.63 + 0)*a/3
I6 =
15.741

-->I = I1 + I2 + I3 + I4 + I5 + I6
I =
120.02733

-->// a lagoa tem aproximadamente 120 Km^2
-->// Questao 2
-->// (a) Quadratura Composta do Trapezio
-->a=0;b=1; n=4; h=(b-a)/n;
-->x0=a;x1=a+h;x2=a+2*h;x3=a+3*h;x4=b; [x0 x1 x2 x3 x4]
ans =
0. 0.25 0.5 0.75 1.

-->function u=f(x)
--> u = 1/(1+exp(x*x));endfunction
-->I1=(f(x0)+f(x1))*h/2,I2=(f(x1)+f(x2))*h/2
I1 =
0.1230475
I2 =
0.1152754

-->I3=(f(x2)+f(x3))*h/2,I4=(f(x3)+f(x4))*h/2
I3 =
0.1000991
I4 =
0.0789888

-->I = I1 + I2 + I3 + I4
I =
0.4174109

-->// (b) Quadratura Composta de Simpson
-->x0m=(x0+x1)/2;x1m=(x1+x2)/2;x2m=(x2+x3)/2;x3m=(x3+x4)/2;
-->[x0 x0m x1 x1m x2 x2m x3 x3m x4]
ans =
column 1 to 6
```

Jan 23, 17 10:47 **p3n162B** Page 2/2

```
0. 0.125 0.25 0.375 0.5 0.625
column 7 to 9
0.75 0.875 1.

-->I1 = (f(x0)+4*f(x0m)+f(x1))*h/6
I1 =
0.1236981

-->I2=(f(x1)+4*f(x1m)+f(x2))*h/6
I2 =
0.1159087

-->I3=(f(x2)+4*f(x2m)+f(x3))*h/6
I3 =
0.1006275

-->I4=(f(x3)+4*f(x3m)+f(x4))*h/6
I4 =
0.0792340

-->I = I1 + I2 + I3 + I4
I =
0.4194684

-->// Questao 3
-->// (a) quadratura de gauss-legendre
-->// x = al*u+be , dx = al*du
-->// 0 = al(-1)+be ==> al = be
-->// 3 = al(1)+be ==> 2 al = 3 ==> al = be = 3/2
-->//int_0^3 f(x)dx= int_{-1}^{1} f(3/2(u+1)) 3/2 du
-->//= int_{-1}^{1} g(u) du, onde g(u)=3/2 f(3/2(u+1))
-->function y=g(u)
--> y = 3/2*f( 3/2*(u+1) );endfunction
-->function u=f(x)
--> u = exp(-x*x); endfunction
-->Ia = 5/9*g(-sqrt(3/5))+8/9*g(0)+5/9*g(sqrt(3/5))
Ia =
0.8845439

-->// (b) quadratura de gauss-legendre
-->// x = al*u+be , dx = al*du
-->// -1 = al(-1)+be ==> be = al - 1
-->// 4 = al(1)+be ==> al + al - 1 = 4 ==> al = 5/2
-->// be = 5/2 - 1 = 3/2 , x = (5u+3)/2, dx=5/2 du
-->//int_{-1}^{1} f(x)dx =int_{-1}^{1} f((5u+3)/2) 5/2 du
-->//= int_{-1}^{1} g(u) du, onde g(u)=5/2 f((5u+3)/2)
-->function u=f(x)
--> u = log(1 + x*x) ; endfunction
-->function y=g(u)
--> y = 5/2 * f( (5*u+3)/2 ); endfunction
-->Ib = 5/9*g(-sqrt(3/5))+8/9*g(0)+5/9*g(sqrt(3/5))
Ib =
6.4033715

-->diary(0)
```